

# Cambridge IGCSE™

# CAMBRIDGE INTERNATIONAL MATHEMATICS Paper 4 (Extended) MARK SCHEME Maximum Mark: 120 Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2020 series for most Cambridge IGCSE<sup>™</sup>, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

This document consists of 8 printed pages.

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# Cambridge IGCSE – Mark Scheme PUBLISHED

# **Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

### GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

### GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

### GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

### GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

# GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Maths-Specific Marking Principles				
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.			
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.			
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.			
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).			
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.			
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.			

### MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

# Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

### **Abbreviations**

answers which round to awrt cao correct answer only dependent dep FT follow through after error ignore subsequent working isw nfww not from wrong working or equivalent oe rounded or truncated rot Special Case SC

seen or implied

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soi

Question	Answer	Marks	Partial Marks
1(a)	$\frac{560}{7}$ ×4 oe	M1	
1(b)	48	2	<b>M1</b> for $\frac{15}{100} \times 320$ oe
1(c)	195	2	<b>M1</b> for $x \times \frac{100 - 8}{100} = 179.40$ oe or better
1(d)	320 – their 48 – 29.60 = 242.40	M1	Clear working to 242.40
	their 240 – 179.40 = 60.60	M1	Clear working to 60.60
	$60.60 \times 4 = 242.40$ cao	A1	Clear statement using 242.40 and 60.60
2(a)	172	3	M2 for $180 - \frac{360}{45}$ or for $\frac{180 \times (45 - 2)}{45}$ or M1 for $\frac{360}{45}$ (implied by 8) or for $180 \times (45 - 2)$ (implied by 7740)
2(b)(i)	75	1	
2(b)(ii)	110	2	<b>B1</b> for angle $CAT = 110$ or angle $CDA = 70$ or <b>M1</b> for $180 - their$ angle $CDA$ .
2(c)(i)	similar	1	
2(c)(ii)	4	3	M2 for $\frac{9}{6} = \frac{AD + 2}{AD}$ oe or M1 for $\frac{AD}{AB} = \frac{6}{9}$ oe
2(c)(iii)	20.25	2	M1 for $\left(\frac{3}{2}\right)^2$ or $\left(\frac{2}{3}\right)^2$ oe seen
3(a)(i)	5	1	
3(a)(ii)	8	1	
3(a)(iii)	7.5	1	
3(a)(iv)	7	1	
3(a)(v)	7.45	2	M1 for at least three of the products $2 \times 5$ , $7 \times 6$ , $11 \times 7$ , $13 \times 8$ , $5 \times 9$ , $2 \times 10$ soi by 298
3(b)(i)	Four points correctly plotted	2	B1 for 2 or 3 correct
3(b(ii)	Positive	1	

Question	Answer	Marks	Partial Marks
3(b)(iii)	0.938x + 0.0405 0.9376 to 0.9377 0.04049 to 0.04050	2	<b>B1</b> for $0.938x + k$ or for $kx + 0.0405$ or for $0.94x + 0.04[0]$
3(b)(iv)	15 or to 15.0 to 15.1	1	FT
3(c)	13.75	2	M1 for at least 3 mid-values seen 5, 12.5, 17.5, 30 implied by 45, 250, 105, 150 or 550
4(a)(i)	20	1	
4(a)(ii)	40	1	
4(b)(i)	50	1	
4(b)(ii)	47	1	
4(b)(iii)	23	1	
4(c)	$\frac{13}{50}$	1	FT their (b)(i)
4(d)	$\frac{3}{175}$ oe	2	M1 for $\frac{7}{their 50} \times \frac{6}{their 50 - 1}$
4(e)	$\frac{7}{187}$ oe	3	M2 for $\frac{7}{34} \times \frac{6}{33}$ or M1 for $\frac{7}{p} \times \frac{6}{p-1}$
5(a)	679.81 or 680 or 679.8	3	<b>M2</b> for $600 \left( 1 + \frac{1.8}{100} \right)^7$ or <b>M1</b> for $600 \left( 1 + \frac{1.8}{100} \right)^k$ , $k > 1$
5(b)	4.2	4	<b>B3</b> for 4.16 or 4.161 to 4.162 or <b>B2</b> for $\sqrt[17]{2}$ oe or <b>M1</b> for $(P) \times ()^{17} = (2P)$ oe

Question	Answer	Marks	Partial Marks
5(c)	6	4	<b>B3</b> for 5.92 or 5.924
			OR
			<b>M3</b> for $n \log \left( 1 - \frac{4}{100} \right) = \log \left( \frac{2120}{2700} \right)$ oe
			or correct trials as far as 5 and 6 or good sketch indicating value between 5 and 6
			or <b>M2</b> for $\left(1 - \frac{4}{100}\right)^n = \frac{2120}{2700}$
			or at least two trials with $n > 2$
			or sketch that could lead to solution e.g. $y = 0.96^x$
			or <b>M1</b> for $2700 \left(1 - \frac{4}{100}\right)^n = 2120$ oe
			or at least 2 correct trials
6(a)	135π	3	<b>M1</b> for $\pi \times 3^2 \times 11$
			M1 for $\frac{4}{3}\pi \times 3^3$
6(b)(i)	3	2	<b>M1</b> for $\pi \times r^2 \times 15 = their$ (a)
6(b)(ii)	2.12 or 2.120 to 2.121	2	<b>M1</b> for $20 \times 10 \times h = their$ (a)
7(a)(i)	(a-b)(a+b)	1	
7(a)(ii)	12.25	5	<b>B4</b> for $2a = 7$ or $2.6a = 9.1$ or better or <b>B3</b> for $2b = 4.4$ or $2.6b = 5.72$ or better
			OR
			<b>M1</b> for $a^2 - b^2 = 7.41$ oe
			M1 for $a - b = 1.3$ oe M1 for $a + b = 7.41 \div 1.3$
			or for a or b correctly eliminated
7(b)(i)	(x-8)(x+3)	2	<b>B1</b> for $(x+a)(x+b)$ with $ab = -24$ or $a+b=-5$
			or for $x(x+3)-8(x+3)$ or for
			x(x-8) + 3(x-8)

Question	Answer	Marks	Partial Marks
Question 7(b)(ii)	Answer 204	Marks 8	Partial Marks  B7 for $x = 8$ isw $x = -3$ OR  M1 for $(x+1)(x+13)$ or for $(x+4)(2x+1)$ B1 for $2x^2 + 8x + x + 4$ B1 for $x^2 + x + 13x + 13$ M1 for $(x+4)(2x+1) - (x+1)(x+13) = 15$ oe  A1 for $x^2 - 5x - 24 = 0$ reached without any error or omission  M1 for $(2 \times their \ x + 1)(their \ x + 4)$ evaluated correctly  OR  M6 for graph(s) which would lead to correct value of $x$ . or M3 for appropriate graph(s) but not leading
			to value of x. or M1 for setting up input for graphics calculator
8(a)(i)	Correct sketch	2	B1 for exponential shape
8(a)(ii)	$0 \le x \le 1.71 \text{ or } 1.709 \text{ to } 1.710$	3	<b>B2</b> for either correct or <b>B1</b> for 0 and 1.71 or 1.709 to 1.710 seen
8(a)(iii)	-1.3[0] or -1.302 0.843 or 0.8429	3	<b>B2</b> for one correct or <b>B1</b> for sketch of $y = x^2$ added to diagram
8(a)(iv)	Two areas shaded which are above $y = 1.5^{-x}$ and below $y = x^2$	1	
8(b)	[a = ] -2 [b = ] -4	3	<b>B1</b> for $a = -2$ <b>M1</b> for $\frac{b}{a} = 2$ oe
8(c)	Correct sketch	3	B1 for each branch

Question	Answer	Marks	Partial Marks
9(a)	$\begin{pmatrix} -3 \\ 4 \end{pmatrix}$	1	
9(b)	(2, 7)	1	
9(c)	(1, 5)	1	
9(d)	(1.5, 6)	1	FT their (b) and (c).
9(e)	2.24 or 2.236	3	FT their (b) and (c). M2 for $(their 2 - their 1)^2 + (their 7 - their 5)^2$ oe or M1 for $(their 2 - their 1)$ and (their 7 - their 5) seen
9(f)	y = 2x - 2  oe	3	M1 for gradient = $\frac{-1}{-\frac{1}{2}}$ oe soi 2 M1 for substituting (3, 4) in $y = their \ m \ x + c$ Answer $2x - 2$ implies M1 M1
10(a)(i)	Rotation 90 [anticlockwise] oe (0, 0) oe	3	B1 for each
10(a)(ii)	Image at (1, -5), (2, -6), (4, -6), (4, -5)	2	<b>B1</b> for reflection in $y = k$
10(a)(iii)	Image at (1, 2), (2, 4), (4, 2), (4, 4)	2	<b>B1</b> for other stretch, factor 2, $y = k$ invariant or y-axis invariant
10(b)	Stretch [factor] 3 x-axis oe invariant	3	<b>B1</b> for each If 0 scored <b>M1</b> for $[g(x)] = 3 \log x$
11(a)	1	2	<b>B1</b> for 3 <sup>2</sup> or 2 <sup>3</sup>
11(b)	-2	1	
11(c)	$\frac{x^4-1}{x^3}$ final answer	2	M1 for $x - \frac{1}{x^3}$
11(d)	$\sqrt[3]{x}$ oe final answer	1	